

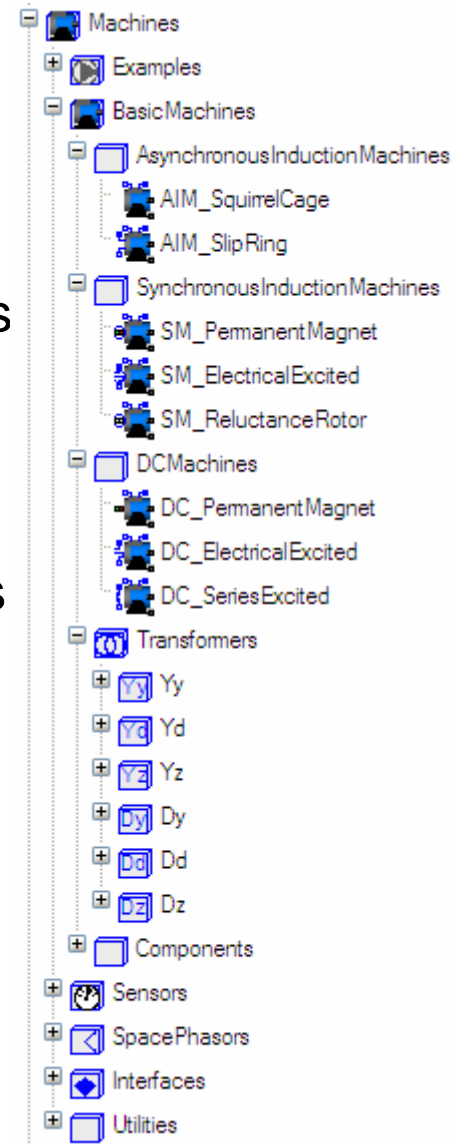
# Object-oriented modeling of electrical machines: Modelica.Electrical.Machines

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arsenal research, Vienna  
03.03.2008



# Contents

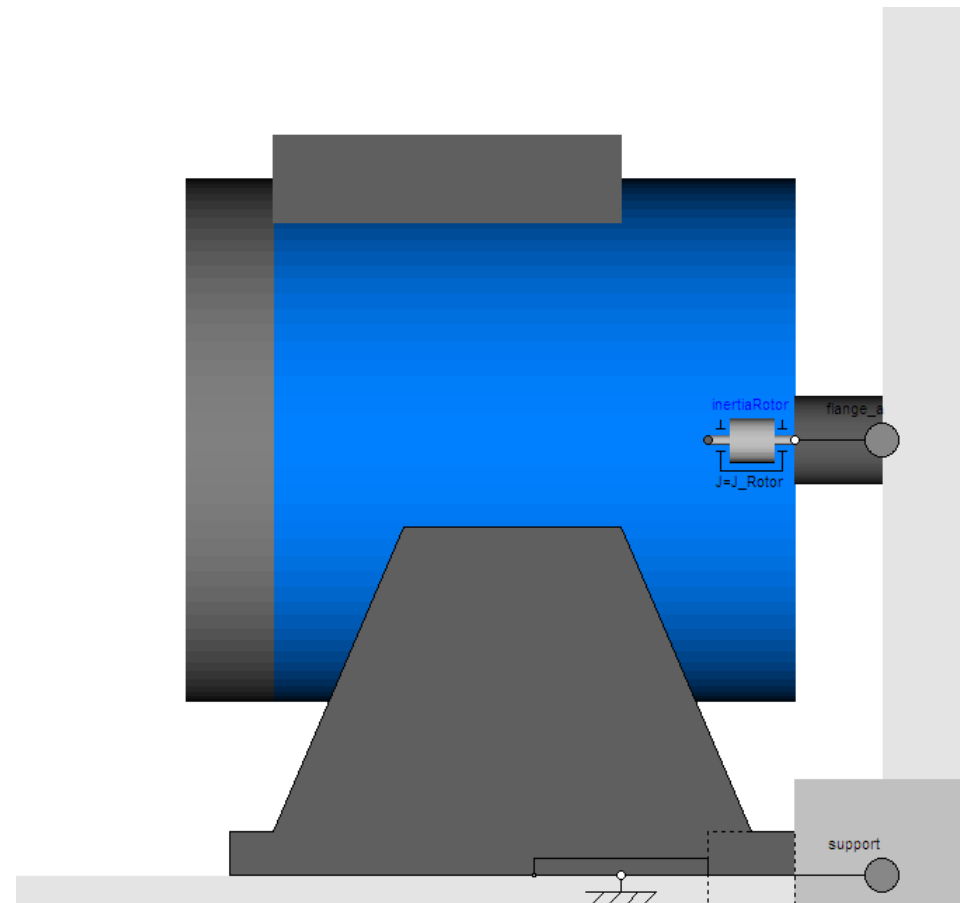
- Common Mechanical Components
- DC Machines
- Induction Machines
- Asynchronous Induction Machines
- Synchronous Induction Machines
- Transformers





# Common Mechanical Components

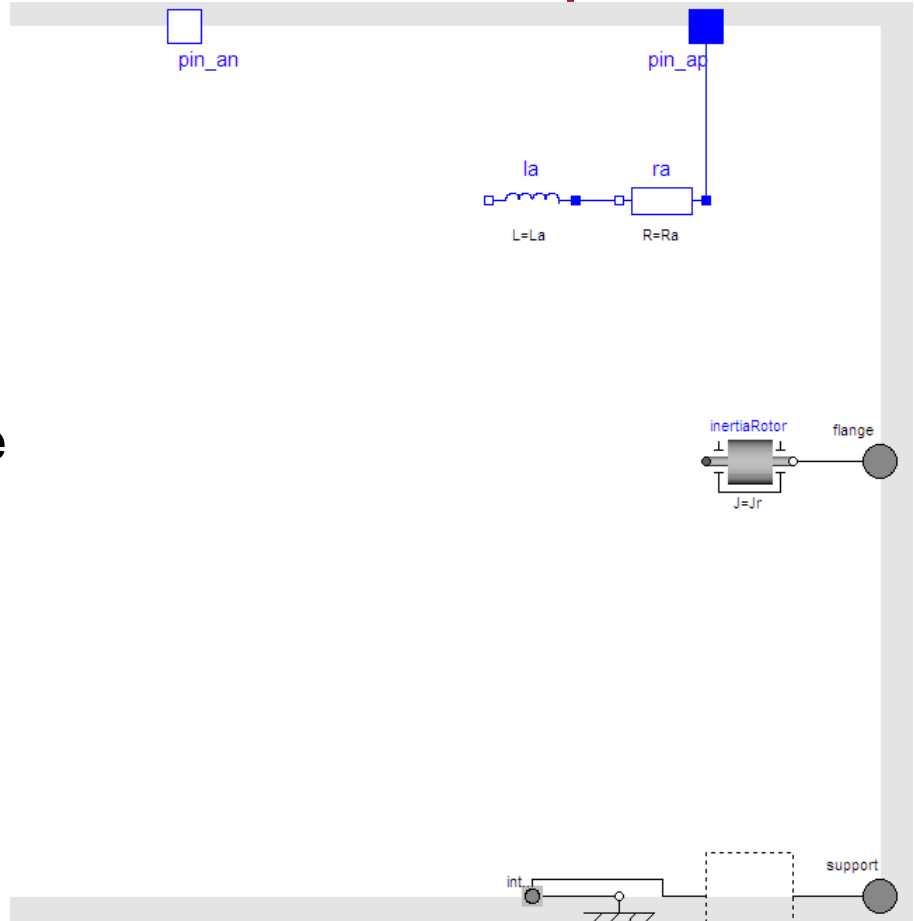
- Rotor's moment of inertia
- Stator:
  - useSupport = false:  
fixed
  - useSupport = true:  
moment of inertia  
+ connect support!
- Common parameters
- Common outputs  
e.g. wMechanical, tauShaft
- Icon





# DC Machines: Common Electrical Components

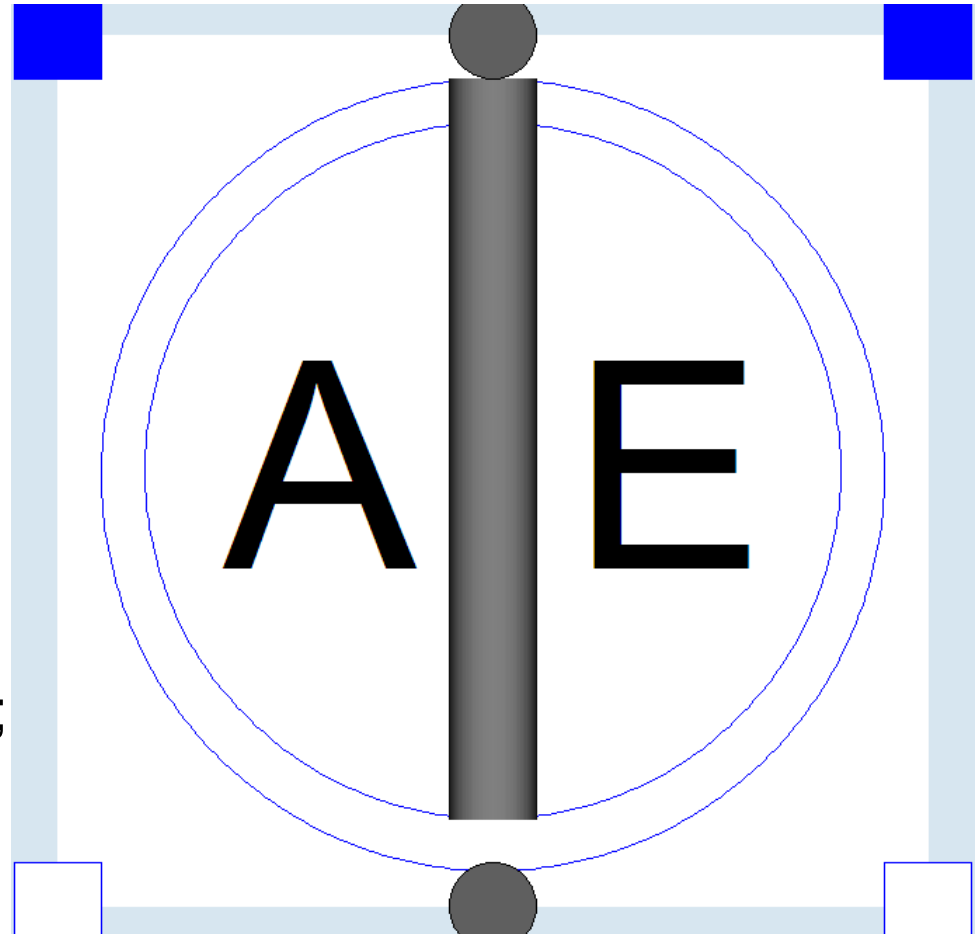
- Armature pins
- Armature resistance + leakage inductance
- Common parameters for:
  - PM DC machine
  - Electrical excited DC machine
  - Series excited DC machine





## DC Machines: Airgap

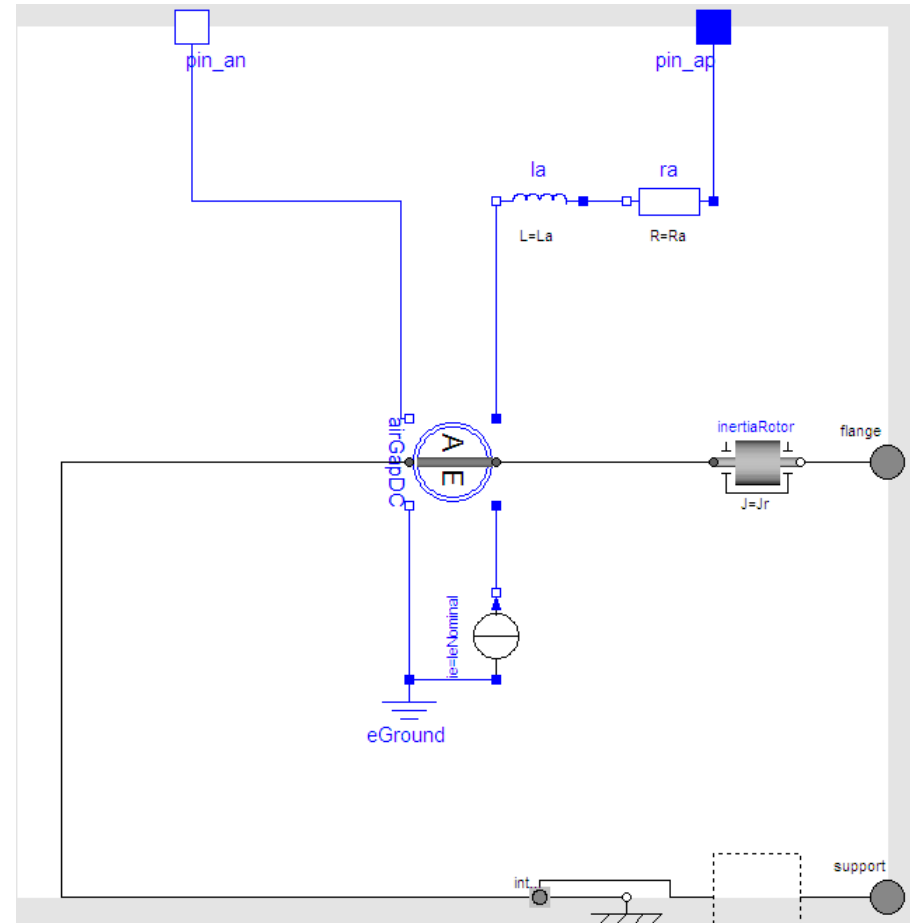
- Calculates flux from excitation current
- Induced armature voltage:  
 $\sim \psi \cdot \omega$
- Induced excitation voltage:  
 $\sim \text{der}(\psi)$
- Torque  $\tau$ :  
 $\sim \psi \cdot \text{armature current}$
- $\omega = \text{der}(\text{shaft.phi} - \text{support.phi})$ ;
- $\tau = - \text{shaft.tau}$ ;  
 $\tau = \text{support.tau}$ ;





# Permanent Magnet DC Machine

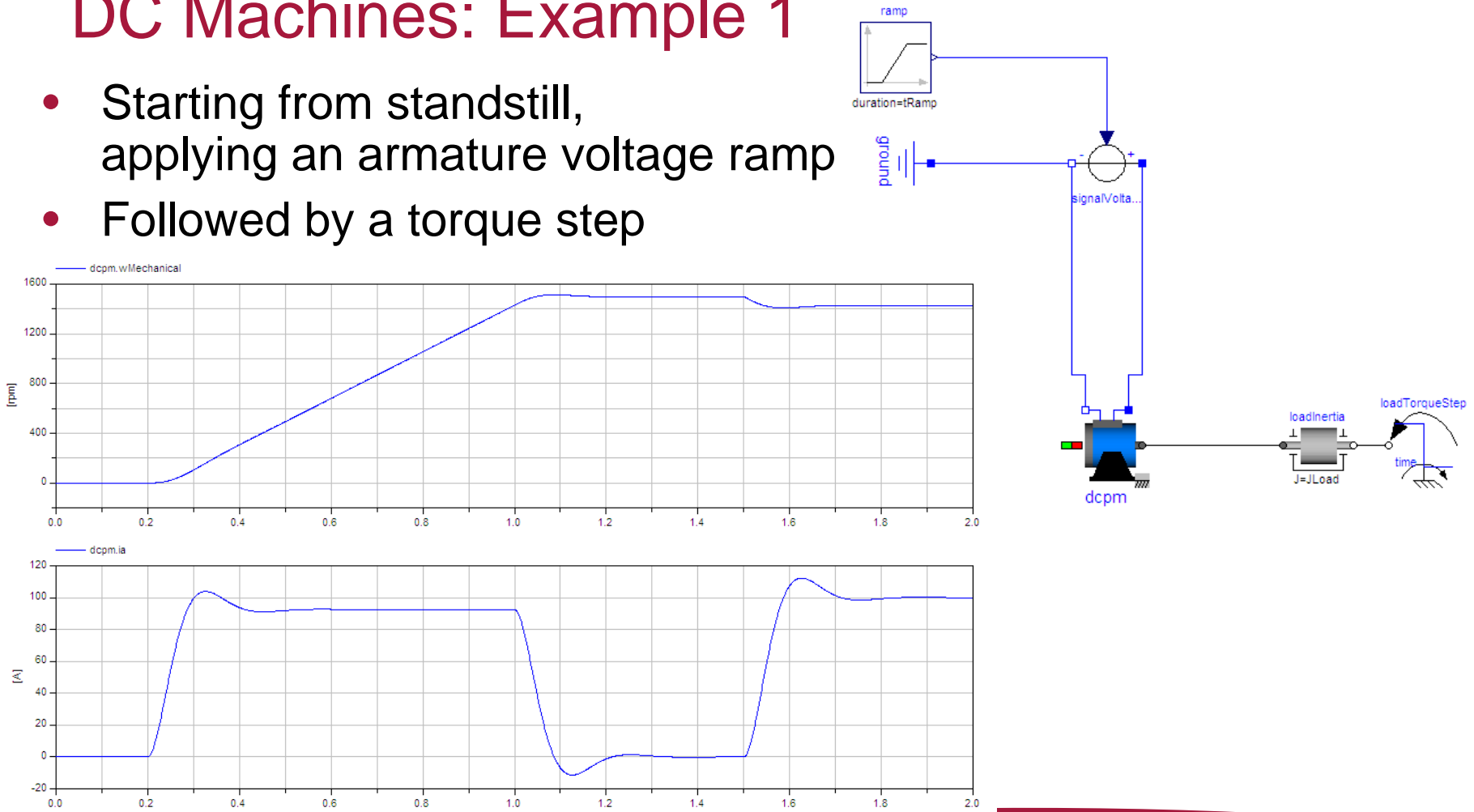
- What's missing:  
excitation
- PM acts like  
constant excitation current
- $\text{turnsRatio} * I_e$ :  
determined by  
induced armature voltage  
at nominal speed  
and no-load





# DC Machines: Example 1

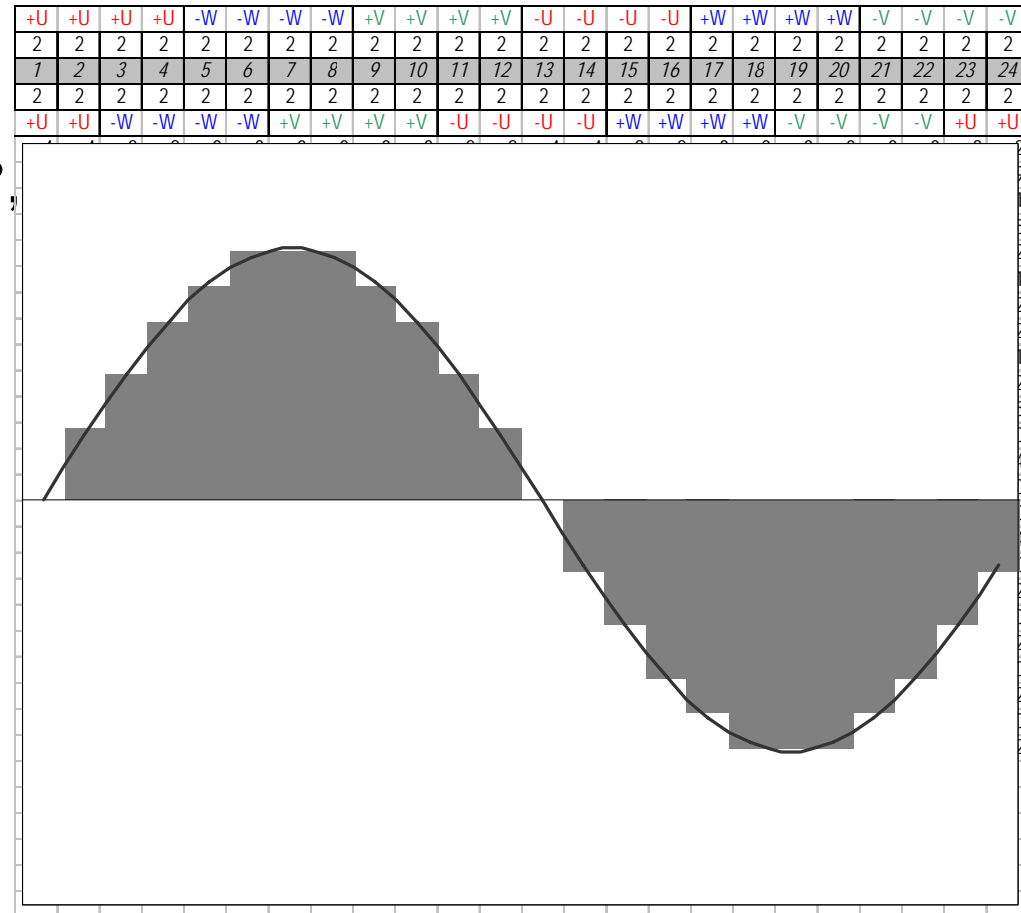
- Starting from standstill, applying an armature voltage ramp
- Followed by a torque step





# Induction Machines: Three-Phase Winding

- Feeding a three-phase winding, i.e. shifted spatially by  $120^\circ$ , with three-phase current, i.e. shifted timely by  $120^\circ$ , gives a sinusoidal field, rotating with  $f / p$ .
- This rotating field can be represented by a **space phasor**.





# Induction Machines: Space Phasors

- Length  $\sim$  field magnitude
- Points to maximum of field
- i.e. rotating with  $f / p$
- Space phasor transformation:  $\underline{a} = e^{j\frac{2\pi}{3}} = \cos\left(\frac{2\pi}{3}\right) + j \cdot \sin\left(\frac{2\pi}{3}\right)$

$$V_0 = \frac{1}{3} \cdot (v[1] + v[2] + v[3])$$

$$\vec{V} = \frac{2}{3} \cdot (\underline{a}^0 \cdot v[1] + \underline{a}^1 \cdot v[2] + \underline{a}^2 \cdot v[3])$$

$$v[1] = V_0 + \operatorname{Re}(\underline{a}^0 \cdot \vec{V})$$

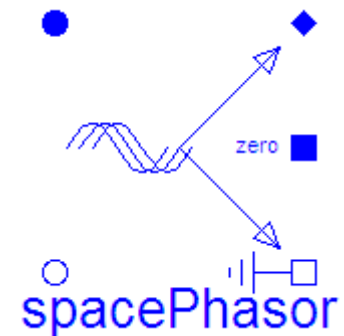
$$v[2] = V_0 + \operatorname{Re}(\underline{a}^2 \cdot \vec{V})$$

$$v[3] = V_0 + \operatorname{Re}(\underline{a}^1 \cdot \vec{V})$$

- coordinate system (2) rotated by the angle  $\gamma$  against the original coordinate system (1):

$$\vec{V}_{(2)} = \vec{V}_{(1)} \cdot e^{-j\gamma}$$

$$\vec{V}_{(1)} = \vec{V}_{(2)} \cdot e^{+j\gamma}$$





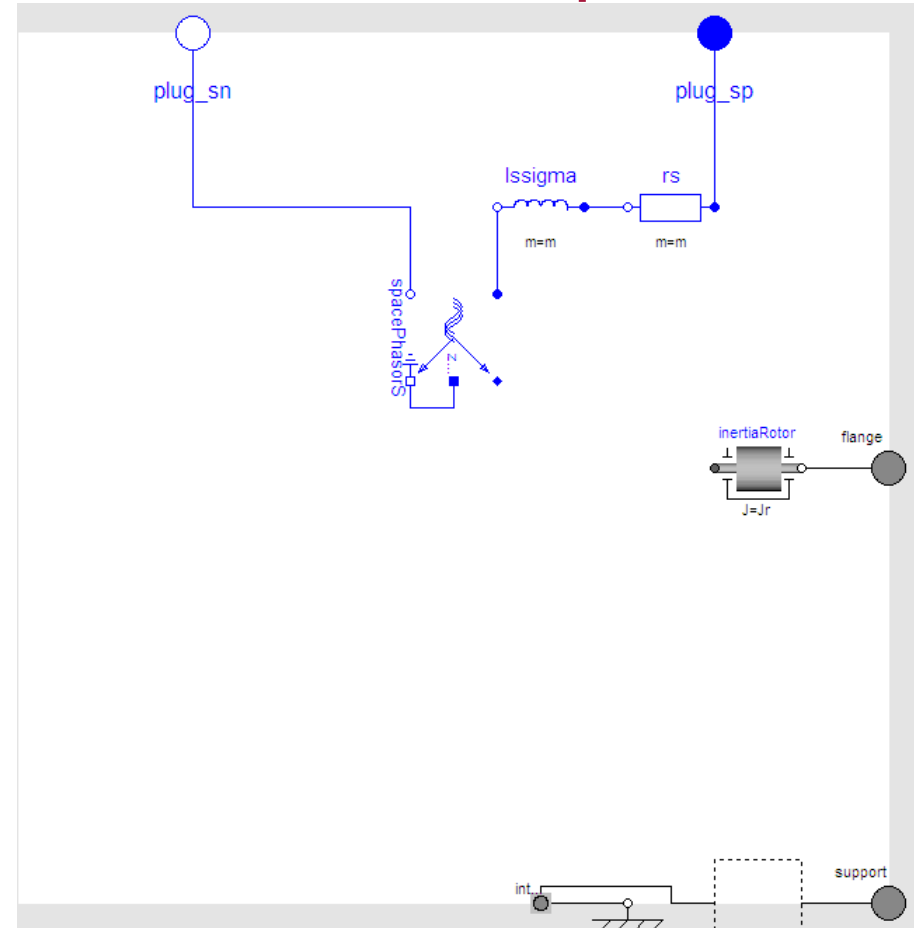
# Assumptions

- Phase symmetric windings are assumed, as well as symmetry of the whole machine structure.
- Only first harmonics (in space) of current coverage, field excitation curve and flux density distribution are taken into account.
- Waveform of all signals is not restricted.
- Resistances and inductances are considered as constant parameters.
- Eddy currents in solid iron as well as iron losses and friction losses are neglected.
- Skin effects are neglected.
- ➔ <http://www.haumer.at/refimg/SpacePhasors.pdf>



# AC Machines: Common Electrical Components

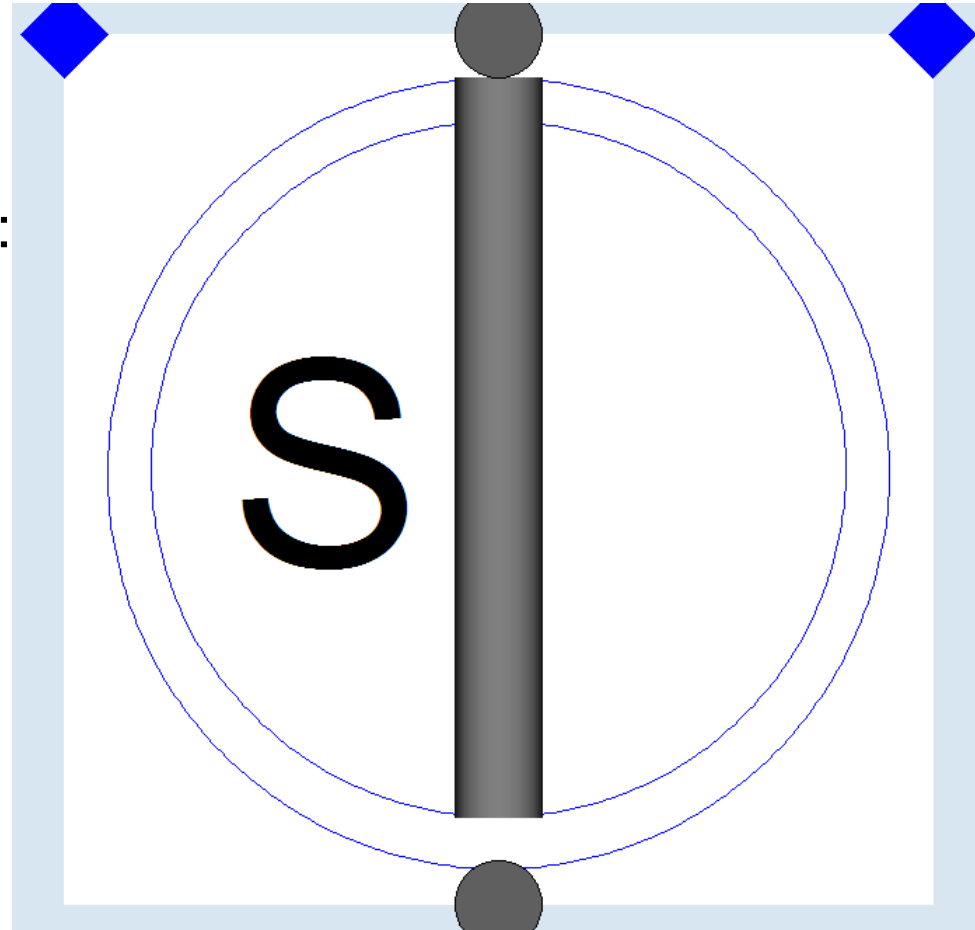
- Stator plugs
- Stator resistances + leakage inductances
- Space phasor transformation
- Common parameters for:
  - AIM squirrel cage
  - AIM slip ring
  - SM permanent magnet
  - SM electrical excited
  - SM reluctance





## AC Machines: Airgap

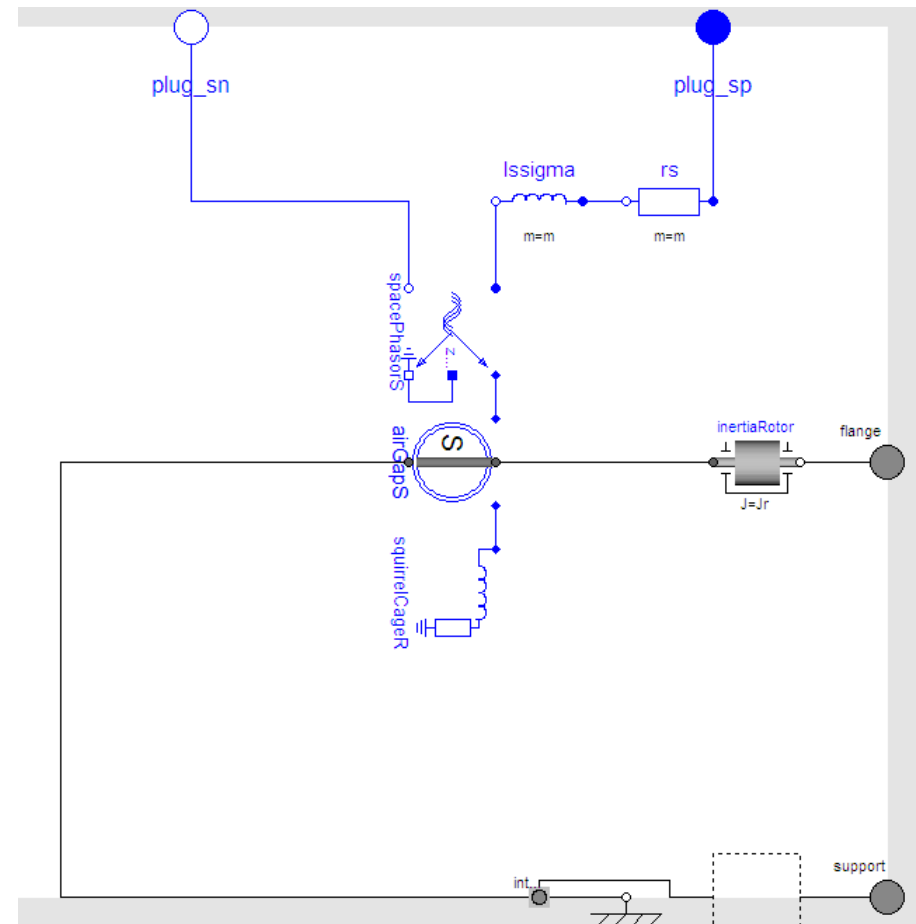
- Calculates main flux from stator + rotor current
- Common coordinate system: stator or rotor fixed
- Induced voltage:  $\text{der}(\psi)$
- Torque tau:  
$$\frac{m}{2} p \cdot \text{Im}(\underline{i}_s \cdot \underline{\psi}_s^*)$$
- $\omega = \text{der}(\text{shaft.phi} - \text{support.phi})$ ;
- $\tau = - \text{shaft.tau}$ ;  
 $\tau = \text{support.tau}$ ;





# AIM Squirrel Cage

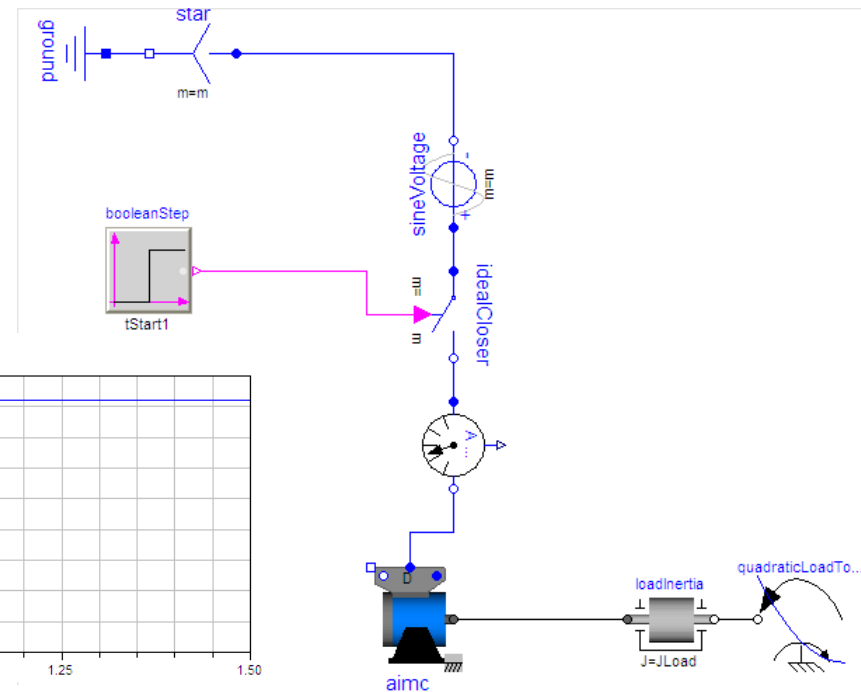
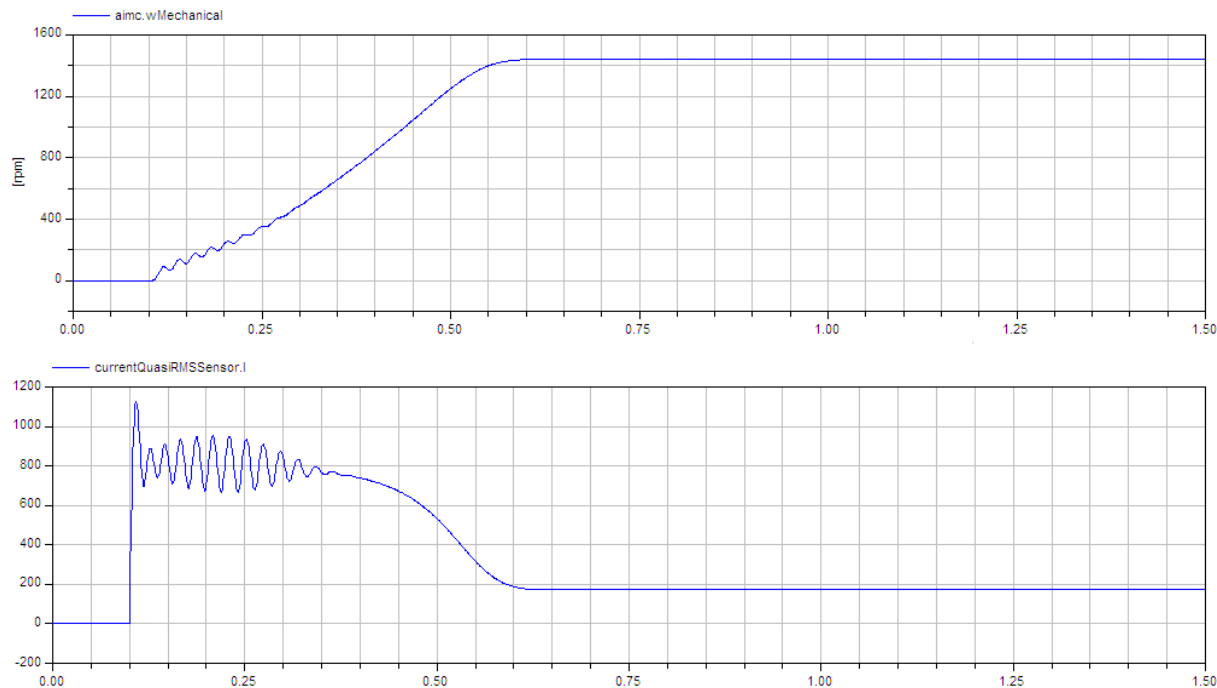
- What's missing: squirrel cage
- resistance and inductance of squirrel cage: w.r.t. stator





# AC Machines: Example 1

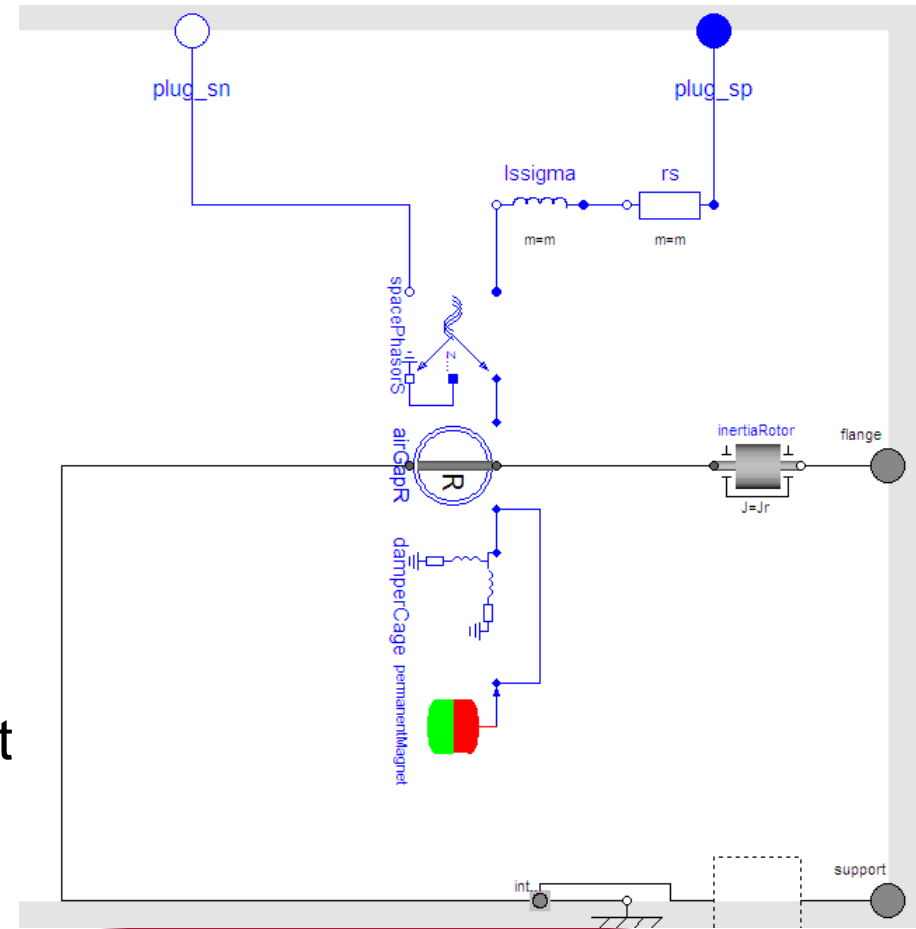
- AIM with squirrel cage
- Starting from standstill
- Quadratic load torque





# SM Permanent Magnet

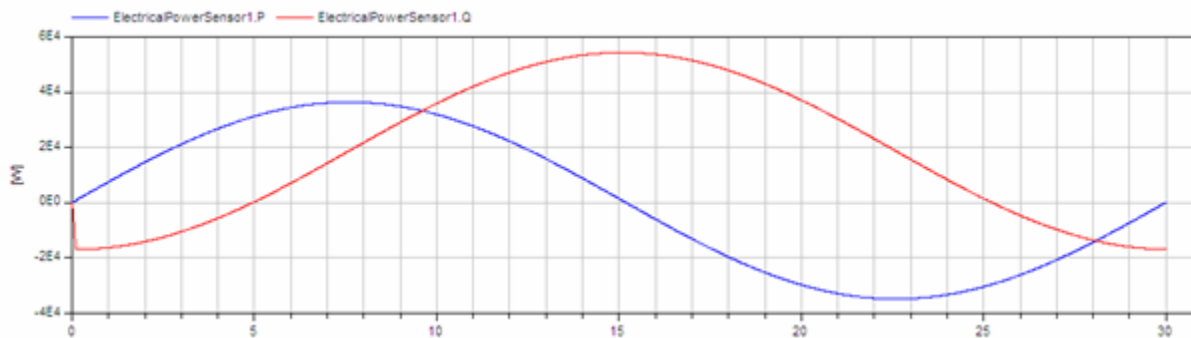
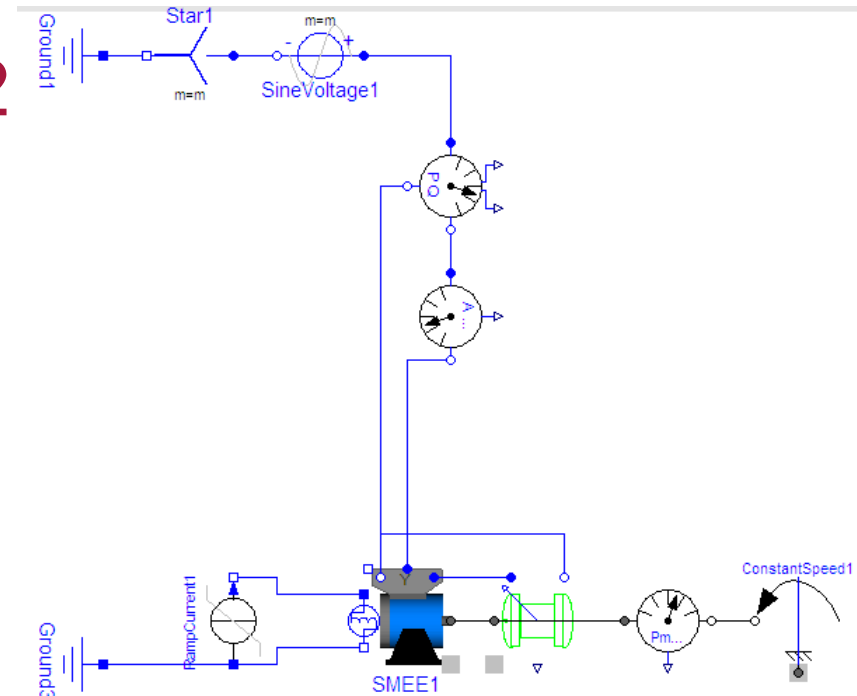
- What's missing: excitation
- PM acts like constant excitation current
- $\text{turnsRatio} * I_e$ : determined by induced stator voltage at nominal speed and no-load
- User can choose whether damper cage is present or not
- Different inductances d-axis and q-axis





## AC Machines: Example 2

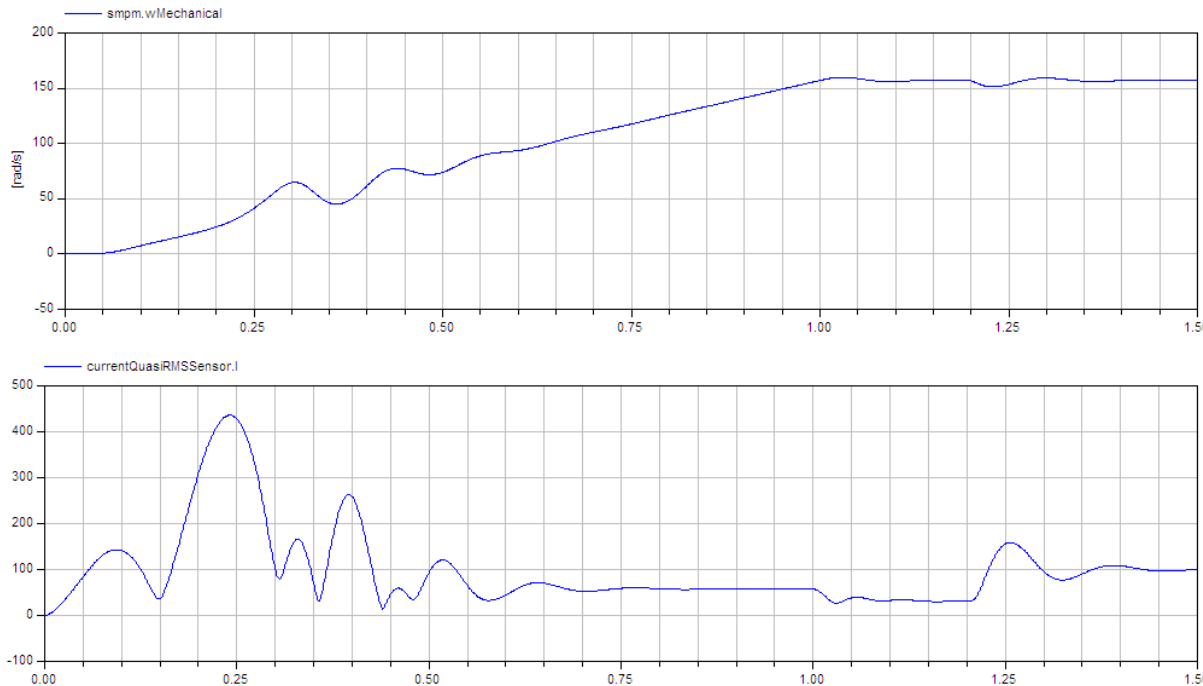
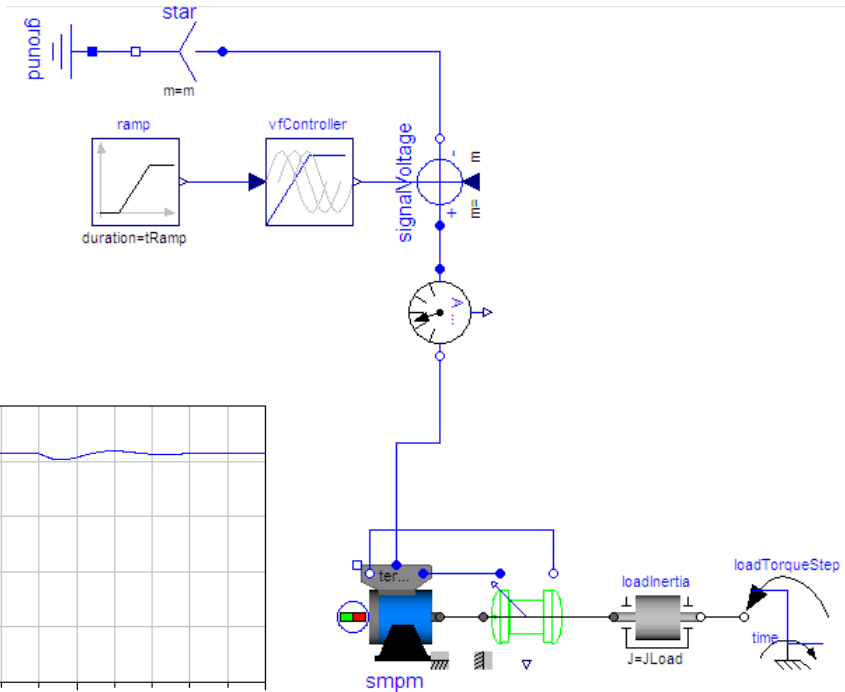
- SM with electrical excitation
- Driven with constant speed
- Constant excitation
- Varying load angle





# AC Machines: Example 3

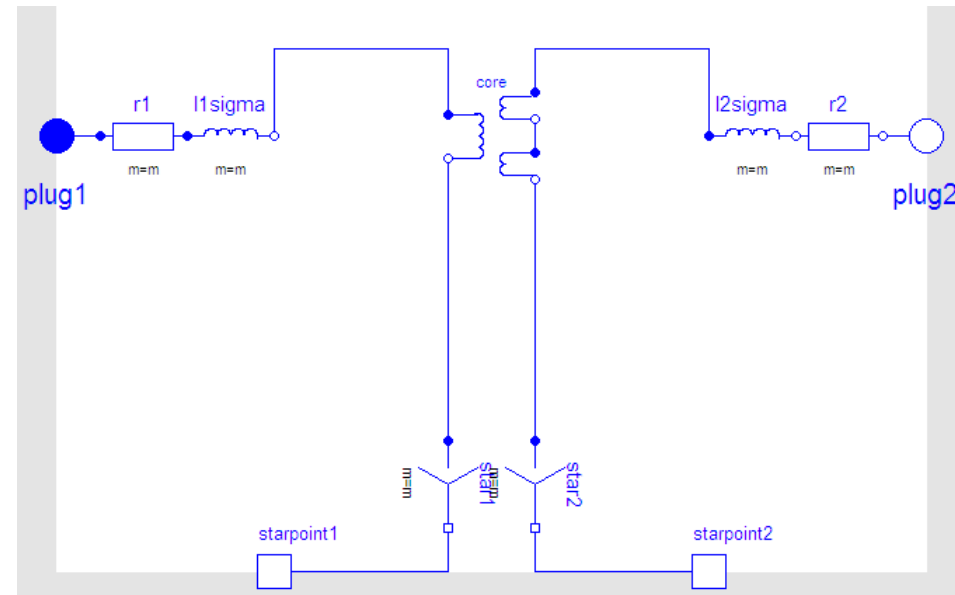
- SM with permanent magnet
- Simple open-loop inverter
- Load torque step





# Transformers

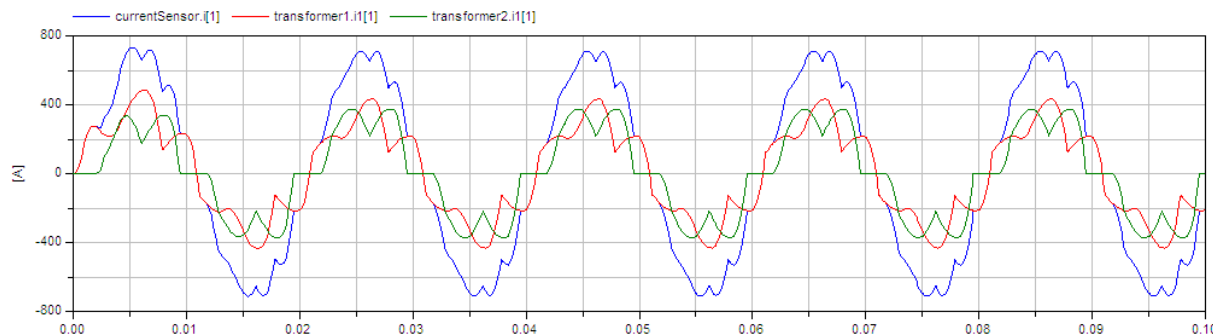
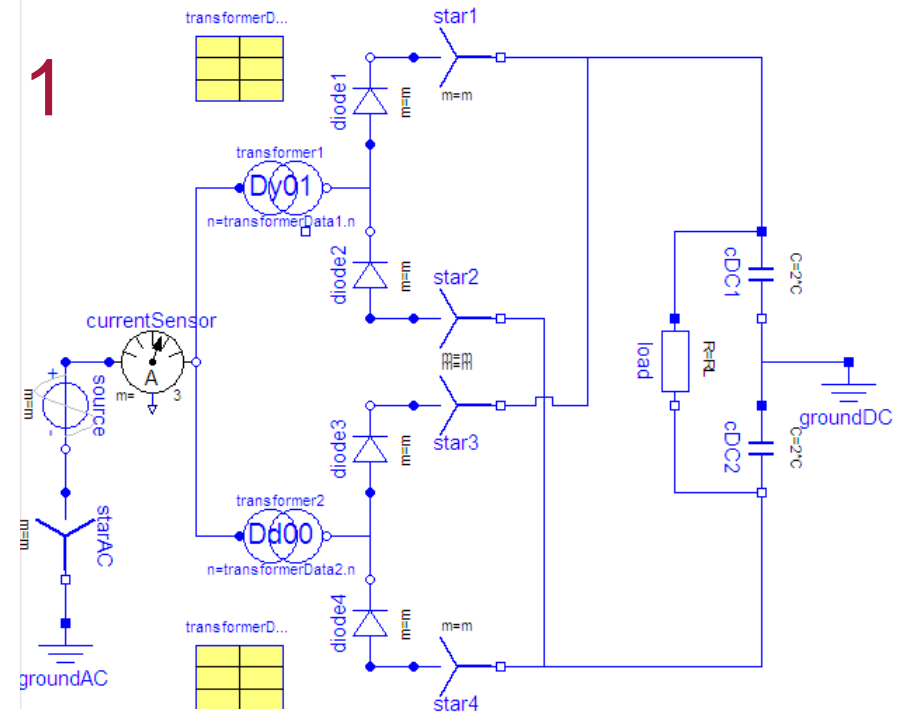
- Primary + secondary resistance + leakage inductance
- No magnetizing current, no magnetizing losses
- Record TransformerData helps to calculate parameters
- All vector groups
  - Yy
  - Yd
  - Yz
  - Dy
  - Dd
  - Dz





# Transformers: Example 1

- 12-pulse rectifier
- Transformer Dy1 + Dd0
- Significant reduction of harmonic currents





# Thank you for your attention.

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web: [www.arsenal.ac.at](http://www.arsenal.ac.at)

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