



# Teaching Modelica® for electrical and mechanical engineers at Technical University of Munich

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Modelica Educational Workshop, 2. April 2009, TU Berlin.

## Lecture: Object-Oriented Modeling of Mechatronic Systems

In winter semester at Technical University of Munich,  
for electrical and mechanical engineering, since 1997, at  
[Lehrstuhl für Elektrische Antriebssysteme und Leistungselektronik](#)  
(1997-2009: Prof. Schröder; since 2009: Prof. Kennel).

### Goal:

Learning the basics of object-oriented modeling at hand of Modelica  
with exercises from the electrical, mechanical, control and thermal domain.  
Practical exercises performed with Dymola.

Number of students:

2008/2009	102 students
2007/2008	68 students
2006/2007	73 students
2005/2006	85 students
2004/2005	61 students

# Organization

- 90 min. lecture once a week
- Exercise once a week. Organized as:
  - 3 times a week, a 90 min. supervised exercise in computer room (20 computers, at most 2 students per computer).
  - I give one of the supervised exercises per week, the other two are given by tutors.
- Exercises are posted on the Web one week beforehand, together with solution (in order that students can check themselves whether it is worth to participate at the supervised exercises).
- Students can install Dymola on their computers and can therefore perform exercises at home
- The students grade is determined in a 60 min. test in the last lecture (some questions are with respect to the exercises).

## Overview of Lectures

### Continuous systems

object diagrams  
differential-algebraic equations (DAE)  
transformation to state space form  
consistent initial conditions of a DAE  
singular DAEs  
integration methods

### Theory

### Discontinuous systems

state and time events  
synchronisation of events  
hierarchical state diagrams  
many ideal switching elements  
Reel/Boolean equation systems

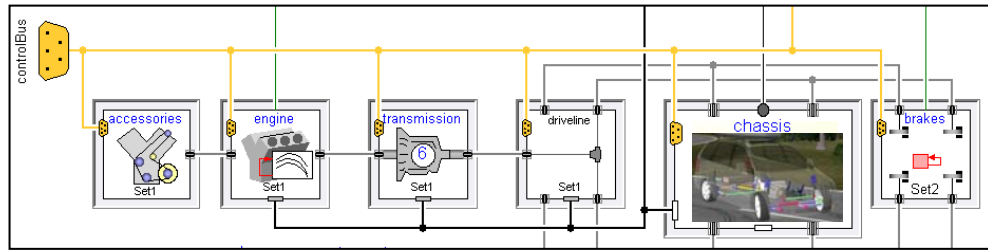
### Applications

Modelica (language) and Dymola (program)  
electrical systems/motors, drive trains,  
3-dim. mechanics, heat transfer,  
input/output blocks,  
inverse models for control systems,  
switching elements (diode, thyristor, friction, ...),  
real-time applications

# 13 Lectures (in 2008/2009)

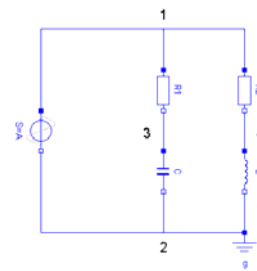
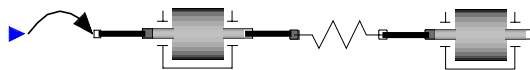
## Lecture 1

Overview, Object diagrams, Modelica Standard Library, introduction into Dymola



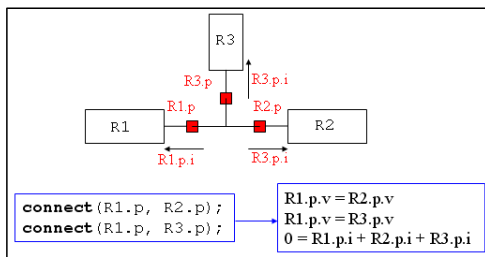
## Lecture 2

Basics of equation based modeling, potential/flow variables, simple examples. How many equations ("balanced models")?



## Lecture 3

Introduction into the Modelica language (textual/graphical Modelica models), connector design (automatic generation of boundary and of balance equations), examples of simple components (capacitor + inertia)

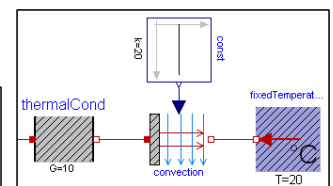
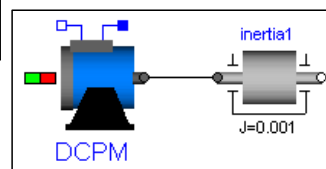
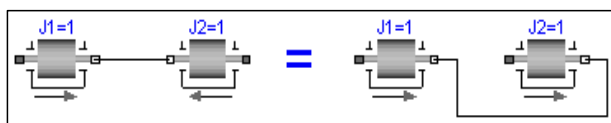


```

model Capacitor
  import SI = Modelica.SIunits;
  parameter SI.Capacitance C;
  SI.Voltage u "Spannungsabfall";
  Pin p, n;
equation
  0 = p.i + n.i;
  u = p.v - n.v;
  C*der(u) = p.i;
end Capacitor;
    
```

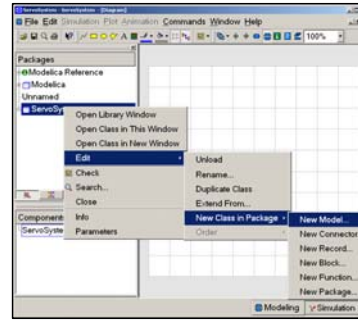
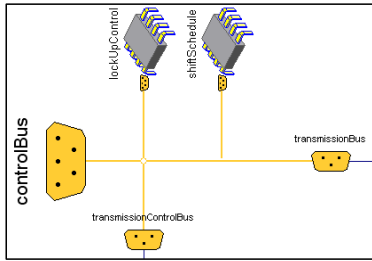
## Lecture 4

Connectors and components for drive trains and heat transfer



## Lecture 5

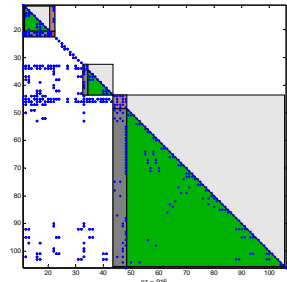
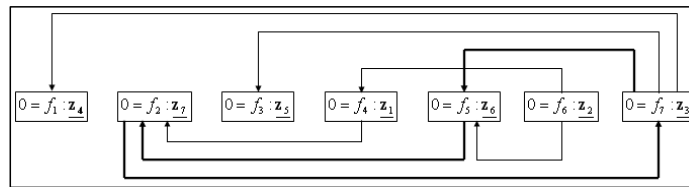
Connectors for signals and buses, hierarchical connectors, inheritance, packages (rename/copy/unload/new...).



## Lecture 6

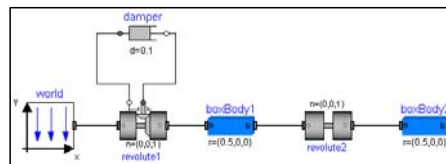
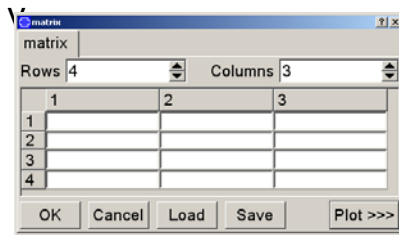
Sorting, i.e. BLT transformation (example, assignment/Tarjan algorithm), variable substitution, i.e., tearing.

$$\begin{aligned} 0 &= f_2(\underline{z}_2) \\ 0 &= f_4(\underline{z}_1, z_2) \\ 0 &= f_3(z_2, \underline{z}_3, \underline{z}_5) \\ 0 &= f_5(z_1, \underline{z}_3, \underline{z}_5) \\ 0 &= f_1(z_3, \underline{z}_4) \end{aligned}$$



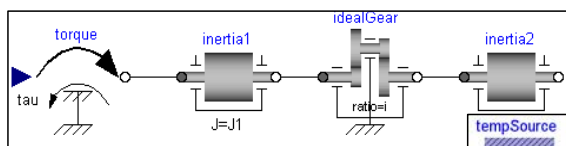
## Lecture 7

Matrices and arrays in Modelica, interfaces and components for multi-body systems, initialization in Modelica

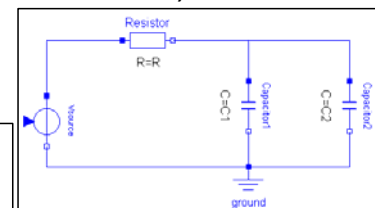
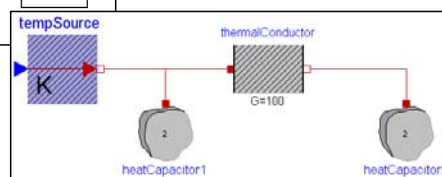


## Lecture 8

Singular systems (examples, Pantelides, dummy derivative method)

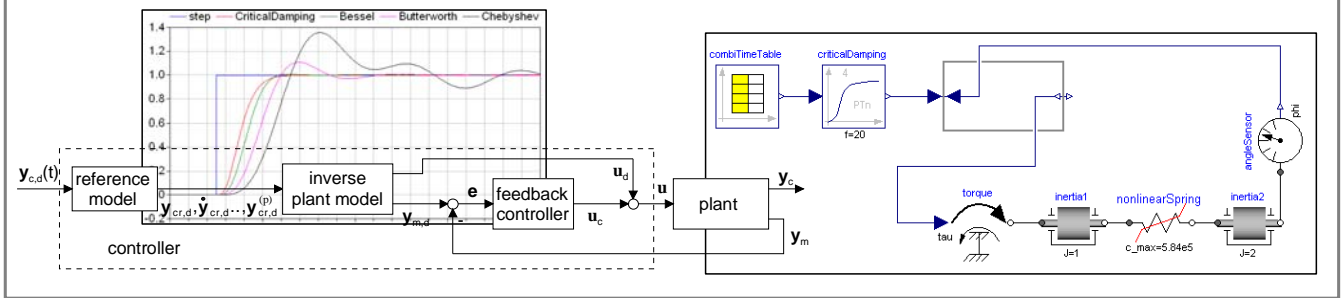


$$\det \left( \frac{\partial \mathbf{f}}{\partial \mathbf{z}} \right) = 0$$



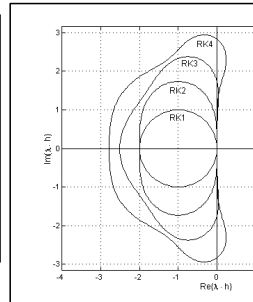
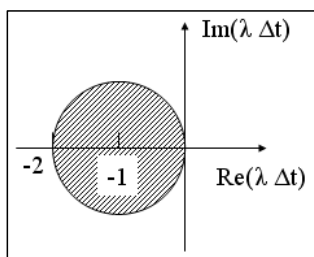
## Lecture 9

Controller with linear, and non-linear inverse model + filter.

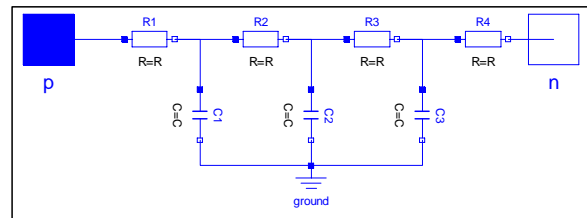


## Lecture 10

Integration methods (explicit/implicit Euler, method order, stability region, examples, Dymolas integrators), component arrays.

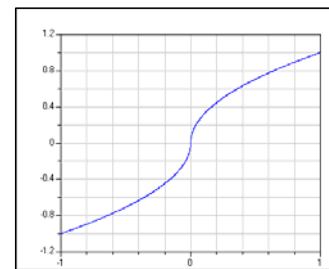
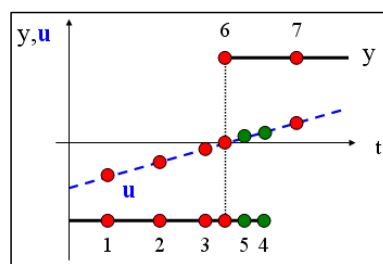
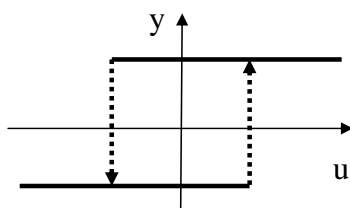


$$|\tilde{\mathbf{x}}(t + \Delta t) - \mathbf{x}(t + \Delta t)| \leq O(\Delta t^{n+1})$$



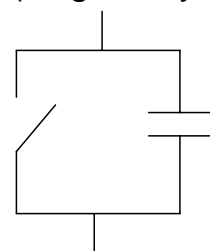
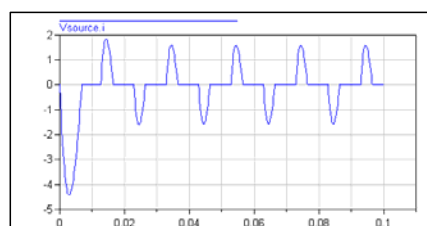
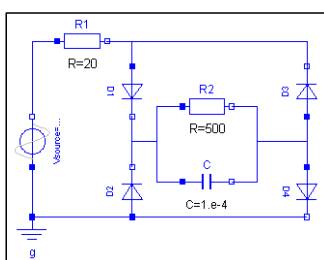
## Lecture 11

Discontinuous systems, state/time events, relation triggered events, pre(..), when, smooth(), noEvent(), synchronous equations (sorting).



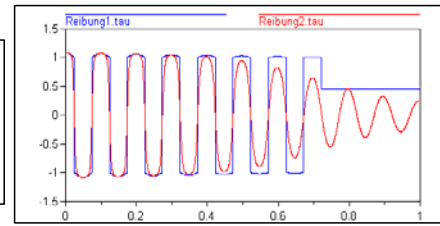
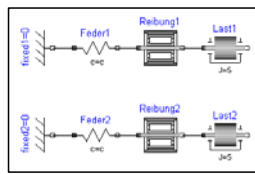
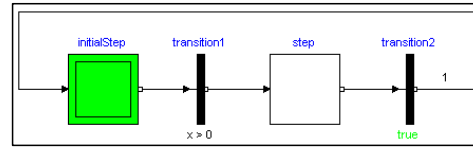
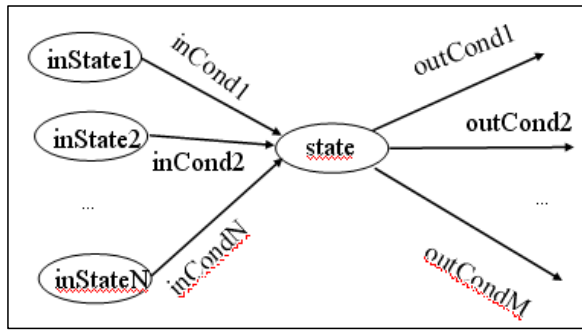
## Lecture 12

Variable structure systems (electrical switch, diode, thyristor, parameterized curve description), Real/Boolean equation systems, problems (singular systems)



# Lecture 13

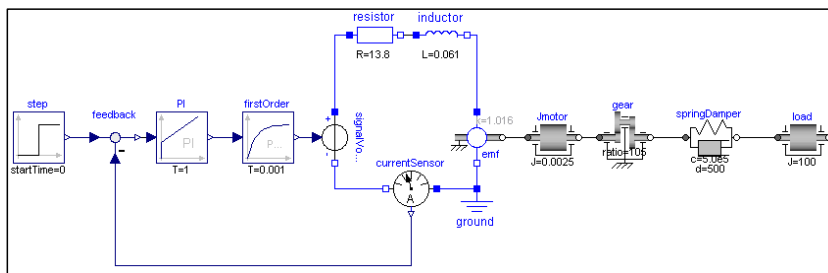
## State diagrams (native implementation, StateGraph), friction



# 9 Exercises (in 2008/2009)

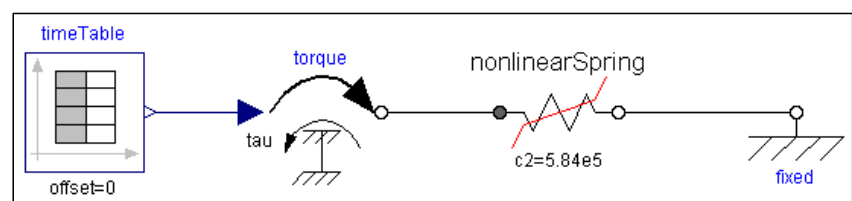
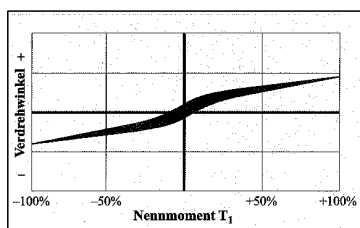
## Exercise 1

Build electrical motor with current controller + elastic load and tune PI coefficients of current controller manually.



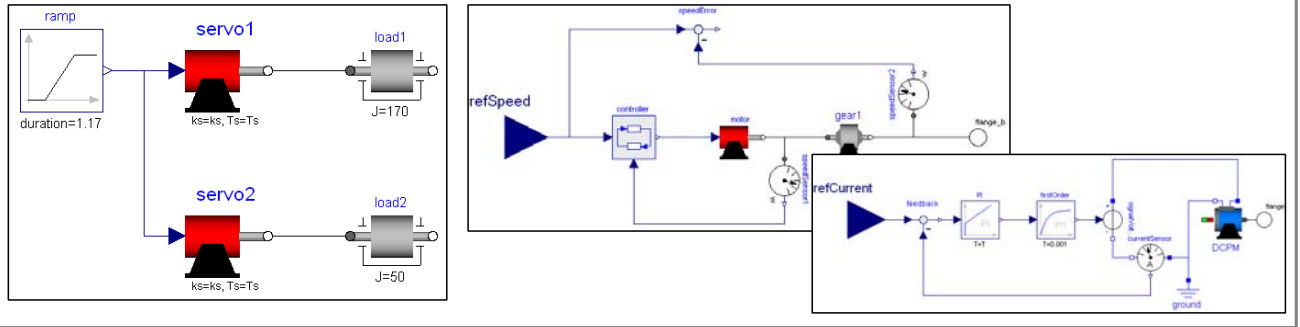
## Exercise 2

Implement and test non-linear spring characteristic



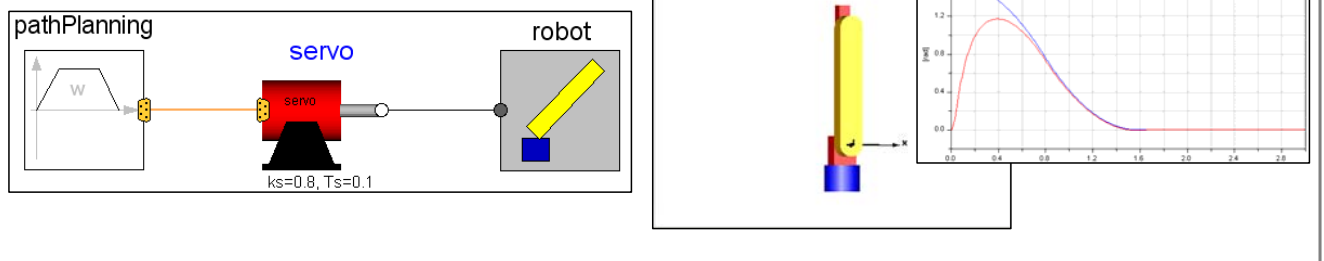
### Exercise 3

Build and tune servo system for two operating points



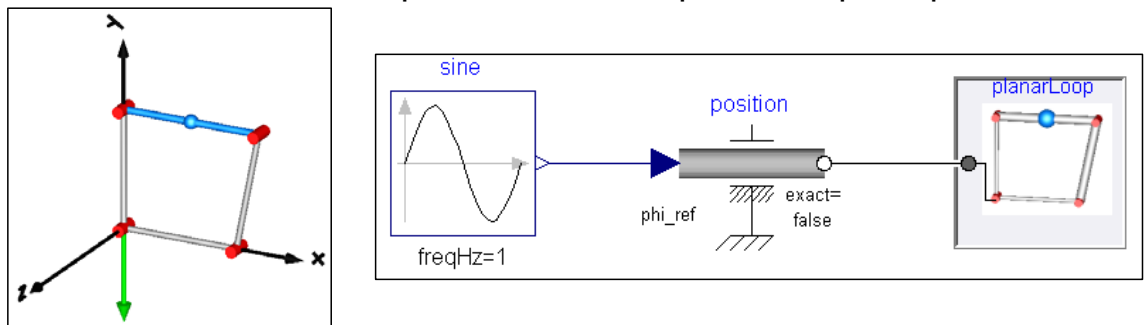
### Exercise 4

Controlled one-arm robot with bus, controller, path planning, steady-state initialization



### Exercise 5

Four-bar mechanism, different implementations of planar loops, replaceable models

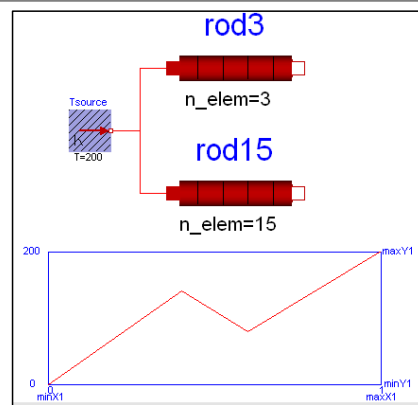
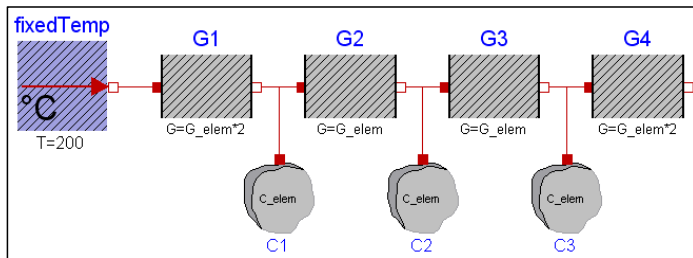


### Exercise 6

Nonlinear robot control with inverse model

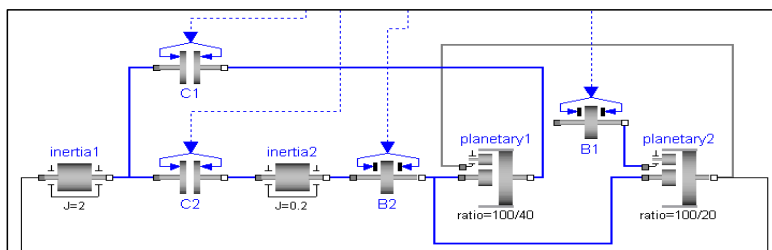
## Exercise 7

### Heat transfer in rod (implementation with vector of components)



## Exercise 8

### Build automatic gearbox and design simple ECU (electronic control unit)



gear	C1	C2	B1	B2
0				
1	on		on	
2	on			on
3	on	on		

## Exercise 9

### Model electrical motor with rectifier, supply source and load

